

# Phonon softening and forbidden mode in $\text{Na}_{0.5}\text{CoO}_2$ observed by Raman scattering

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Polarized Raman scattering measurements have been performed on  $\text{Na}_{0.5}\text{CoO}_2$  single crystal from 8 to 305 K. Both the  $A_{1g}$  and  $E_{1g}$  phonon modes show a softening below  $T_{c1} \approx 83$  K. Additionally, the  $A_{1g}$  phonon mode, which is forbidden in the scattering geometry of cross polarization for the triangular  $\text{CoO}_2$  layers, appears below  $T_{c1}$ . In contrast, the metal-insulator transition at  $T_{c2} \approx 46$  K has only secondary effect on the Raman spectra. The phonon softening and the “forbidden” Raman intensity follow closely magnetic order parameter and the gap function at the Fermi surface, indicating that the distortion of  $\text{CoO}_6$  octahedra at  $T_{c1}$ , instead of the Na ordering at  $\sim 350$  K, is the relevant structural component of the 83 K phase transition.

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## I. INTRODUCTION

The layered cobaltates  $\text{Na}_x\text{CoO}_2$  are well known for their ionic mobility.<sup>1</sup> Recently, their electronic properties have attracted much interest due to the discovery of superconductivity when water is intercalated.<sup>2</sup> The Co ions form a triangular lattice in the  $\text{CoO}_2$  planes, which are separated by  $\text{Na}^+$  ions. With varying  $\text{Na}^+$  content  $x$ , the valence of Co ions can be tuned from  $\text{Co}^{4+}$  (low spin  $S=1/2$ ) to  $\text{Co}^{3+}$  ( $S=0$ ). Analogy to the high transition-temperature cuprate superconductors has been drawn, since  $\text{Na}_x\text{CoO}_2$  may be regarded as doping a  $S=1/2$  Mott insulator on a triangular lattice.<sup>2</sup> However, the  $\text{Na}^+$  layers serve not only as charge reservoirs. Order of  $\text{Na}^+$  ions at specific concentrations dramatically affect electronic properties, such as the insulating state at  $x=0.5$  sandwiched by metallic states at lower and higher dopings.<sup>3,4</sup> Additionally, the valence of Co ions in the hydrated superconductor  $\text{Na}_{0.35}\text{CoO}_2 \cdot 1.3\text{H}_2\text{O}$  is suggested in recent studies to be close to  $+3.5$  rather than the apparent  $+3.7$ , caused by the isovalent exchange of the hydronium ion  $\text{H}_3\text{O}^+$  and  $\text{Na}^+$ .<sup>5,6</sup> Hence,  $\text{Na}_x\text{CoO}_2$  with  $x=0.5$  instead of  $x \sim 0$  may be regarded as the parent compound of the hydrated superconductor. Therefore, it is of particular interest to focus on  $\text{Na}_{0.5}\text{CoO}_2$ .

A metal-insulator transition (MIT) at  $T_{c2} \sim 51$  K is clearly indicated in transport and infrared measurements of  $\text{Na}_{0.5}\text{CoO}_2$ .<sup>3,7</sup> The transition is marked also by a depression in magnetic susceptibility. In addition, another anomaly in magnetic susceptibility occurs at  $T_{c1} \sim 88$  K, where the spins form an alternating antiferromagnetic pattern in the  $\text{CoO}_2$  plane<sup>8,9</sup> and the Hall coefficient abruptly changes sign.<sup>3</sup> The MIT has been explained as a consequence of charge ordering,<sup>3</sup> and structure data from electron and neutron diffraction measurements have been explained by alternating  $\text{Co}^{3.5+\delta}$  and  $\text{Co}^{3.5-\delta}$  chains, decorated by an ordered  $\text{Na}^+$  pattern which exists already at the room temperature.<sup>4,10</sup> However, the charge segregation into  $\text{Co}^{3.5\pm\delta}$  is disputed by a

recent NMR study, and an alternative explanation of nesting of the Fermi surface at the lower orthorhombic symmetry is provided.<sup>11</sup> The nesting of the Fermi surface is also used to explain the angle-resolved photoemission spectroscopy (ARPES) experiments.<sup>12</sup> The subtle relation between electronic, magnetic, and structural properties also manifests in the restoration of the triangular symmetry of  $\text{Na}_{0.5}\text{CoO}_2$  at high magnetic fields.<sup>13</sup>

Although a link between  $\text{Na}^+$  ordering, which breaks the triangular symmetry, and the phase transitions at  $T_{c1}$  and  $T_{c2}$  in  $\text{Na}_{0.5}\text{CoO}_2$  have been suggested through Co charge segregation, the relation between structure and the successive transitions cannot be unambiguously determined in the crystallography studies due to the limited sensitivity of the diffraction techniques.<sup>4,10</sup> In addition, no anomaly in lattice dynamics has been reported at these transitions in  $\text{Na}_{0.5}\text{CoO}_2$ . Here we present polarized Raman scattering measurements on single crystalline sample of  $\text{Na}_{0.5}\text{CoO}_2$  from 8 to 305 K. Phonon softening is observed below  $T_{c1}$  for both the  $A_{1g}$  and  $E_{1g}$  modes of the  $\text{CoO}_6$  octahedra. Simultaneously, the forbidden  $A_{1g}$  mode in the channel of cross polarization appears at  $T_{c1}$ . It indicates that the transition at  $T_{c1}$  is not only magnetic or electronic, but also involved with structural distortion of the  $\text{CoO}_6$  octahedra. The distortion in the  $\text{CoO}_2$  plane, instead of the orthorhombic Na ordering at  $\sim 350$  K,<sup>3,4</sup> is more directly related to the phase transition probed in the NMR, ARPES, and neutron diffraction experiments at  $T_{c1}$ .

## II. EXPERIMENTAL DETAILS

Single crystal samples of  $\text{Na}_x\text{CoO}_2$  were grown using a traveling solvent floating-zone furnace. The as-grown crystal was cut into pieces with the dimensions of  $\sim 2 \times 2 \times 0.2$  mm<sup>3</sup> and has a starting sodium concentration of about 0.75. After the chemical deintercalation of Na in solutions of  $\text{I}_2$  dissolved acetonitrile, the actual Na concentration was determined to be  $x=0.5 \pm 1\%$  by inductively

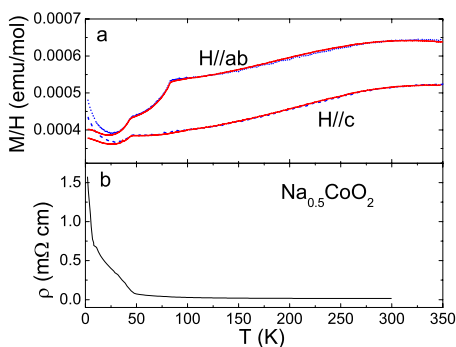


FIG. 1. (Color online) Temperature dependence of (a) magnetic susceptibility and (b) in-plane resistivity of  $\text{Na}_{0.5}\text{CoO}_2$ . The blue dashed and red solid curves in (a) were measured in magnetic fields of 1 and 12 T, respectively.

coupled plasma spectrometry. The detailed procedure for preparing high-quality single crystal samples can be found elsewhere.<sup>14</sup> The susceptibility and resistivity of the  $\text{Na}_{0.5}\text{CoO}_2$  single crystal used in the Raman study are shown in Fig. 1. They are in good agreement with published results,<sup>3,7-12</sup> with  $T_{c2} \approx 46$  K and  $T_{c1} \approx 83$  K.

The Raman measurements were performed with a double-grating monochromator (Jobin Yvon U1000). The detector is a back-illuminated charge-coupled device cooled by liquid nitrogen. An argon ion laser was used with an excitation wavelength of 514.5 nm. The laser beam of 3 mW was focused into a spot of  $\sim 70$   $\mu\text{m}$  in the diameter on the sample surface. The temperature increase by laser heating is less than 10 K and was calibrated in the measurements. The sample was mounted in a liquid helium cryostat with a vacuum of  $\sim 10^{-7}$  torr. The data were collected with a pseudobackscattering configuration. Perfect surface was obtained after cleavage, and the crystal orientation was determined by the Laue pattern before the sample was mounted in the cryostat.

### III. RESULTS AND DISCUSSIONS

The edge-shared  $\text{CoO}_6$  octahedra in  $\text{Na}_x\text{CoO}_2$  form triangular planes.<sup>10</sup> The polarization of light along the Co-O bond orientation is denoted as  $x$ , and the perpendicular orientation in the  $\text{CoO}_2$  plane as  $y$ . A standard calculation of the Raman tensors shows that the in-plane  $E_{1g}$  mode of oxygen vibrations in the  $\text{CoO}_6$  octahedra is allowed in both the  $xx$  and  $xy$  channels. The out-of-plane  $A_{1g}$  mode, however, is allowed only in the  $xx$  channel. Polarized Raman spectra in the  $xx$  and  $xy$  channels, measured at various temperatures, are shown in Fig. 2. The wave numbers of the  $E_{1g}$  and  $A_{1g}$  modes are 469 and 572  $\text{cm}^{-1}$ , respectively, at 305 K. They are consistent with published data on  $\text{Na}_x\text{CoO}_2$  and  $\text{Na}_x\text{CoO}_2 \cdot y\text{H}_2\text{O}$ ,<sup>15-17</sup> and first-principles calculations.<sup>18,19</sup>

The wave numbers of the  $E_{1g}$  and  $A_{1g}$  modes are shown in Fig. 3 as a function of temperature. As the sample was cooled from the room temperature to  $T_{c1}$ , the phonon wave numbers of both modes increase gradually. The increase can be understood naturally in terms of anharmonic effect which

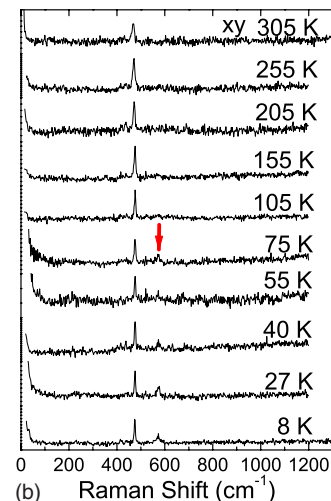
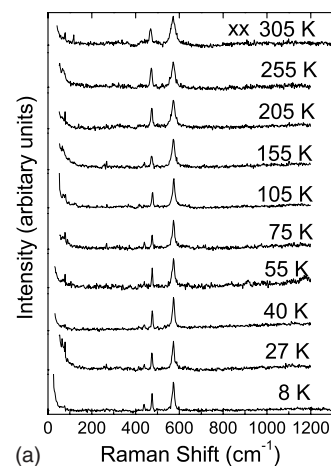


FIG. 2. (Color online) Polarized Raman spectra at various temperatures. (a) In the  $xx$  channel, both  $E_{1g}$  and  $A_{1g}$  modes are allowed. (b) In the  $xy$  channel, only the  $E_{1g}$  mode is active. However, the forbidden  $A_{1g}$  mode near 573  $\text{cm}^{-1}$  grows in the  $xy$  channel below  $T_{c1} \approx 83$  K, as indicated by the arrow.

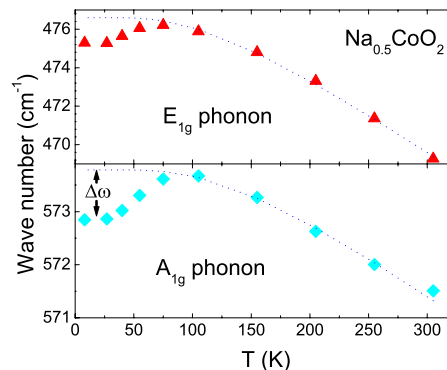


FIG. 3. (Color online) Temperature dependence of the  $E_{1g}$  and  $A_{1g}$  phonon wave numbers. The dotted curves are the least-square fitting of data taken above 83 K to Eq. (1) for anharmonic effect, and phonon softening  $\Delta\omega$  occurs below  $T_{c1}$ .

has also been reported previously.<sup>16</sup> It includes two contributions: one from thermal expansion and the other from multiphonon decay process.<sup>20,21</sup> The contribution from thermal expansion can be written as  $-3\omega_0\gamma\Delta a/a$ , where  $\omega_0$  is the zero-temperature phonon frequency,  $\gamma$  the Grüneisen constant, and  $\Delta a/a$  the linear thermal expansion.<sup>22,23</sup> Neutron diffraction shows that the average in-plane  $\Delta a/a$  is 16 ppm, whereas  $\Delta a/a$  is 2540 ppm for the  $c$  axis.<sup>24</sup> Since the  $E_{1g}$  ( $A_{1g}$ ) phonon mode is related to the in-plane (out-of-plane) vibrations of oxygen atoms in the  $\text{CoO}_6$  octahedra, the wave numbers should be sensitive to the change of the in-plane bonds rather than the  $c$ -axis expansion. Hence, the small in-plane  $\Delta a/a$  would translate to a small anharmonic contribution from thermal expansion.

The main contribution to the shift of phonon wave numbers above  $T_{c1}$  then can be reasonably attributed to multiphonon decay process. For a three-phonon process, a Raman optical phonon with the frequency of  $\omega_0$  will decay into two phonons with  $\omega_1$  and  $\omega_2$ , respectively, where  $\omega_0 = \omega_1 + \omega_2$ . The frequency shift by the process is

$$\omega - \omega_0 = -\alpha \left( \frac{1}{e^{\omega_1/kT} - 1} + \frac{1}{e^{\omega_2/kT} - 1} \right), \quad (1)$$

where  $\alpha$  is a material-dependent constant.<sup>20,25</sup> Klemens has considered the decay channels through acoustic phonons which fulfill the condition  $\omega_1 = \omega_2$ .<sup>21</sup> In many cases, it offers a good approximation. The dotted curves in Fig. 3 are the results of fitting data above  $T_{c1}$  to Eq. (1) under the Klemens condition with  $\alpha = 7.5$  and  $3.5 \text{ cm}^{-1}$  for the  $E_{1g}$  and  $A_{1g}$  modes, respectively. The Klemens model describes well our data above  $T_{c1}$ , and the values of  $\alpha$  are comparable with  $13 \text{ cm}^{-1}$  deduced from diamond, and  $2\text{--}4 \text{ cm}^{-1}$  for semiconducting materials such as AlN, Si, and GaAs.<sup>25,26</sup>

When the sample was cooled further, we observed in this work that both the  $E_{1g}$  and  $A_{1g}$  modes soften considerably below the  $T_{c1}$ , departing from the dotted curves from the anharmonic effect (Fig. 3). The softening in frequency,  $\Delta\omega$ , is taken as the difference between the dotted curve and measured data. It is scaled so that it has the same value at 8 K for both the  $E_{1g}$  and  $A_{1g}$  modes, and it follows the same function of temperature for both modes as shown in Fig. 4.

Since an antiferromagnetic transition occurs at  $T_{c1}$ , it is natural to consider the spin-phonon coupling. In a magnetic material mediated by the superexchange interaction  $J$ , such as in magnetic insulators, the  $J$  would be modulated by the vibrating positions of ligands as follows:

$$J(\mathbf{r}) = J(\mathbf{r}_0) + \frac{\partial J}{\partial \mathbf{r}} \Big|_{\mathbf{r}_0} \cdot (\mathbf{r} - \mathbf{r}_0) + \frac{\partial^2 J}{\partial \mathbf{r}^2} \Big|_{\mathbf{r}_0} (\mathbf{r} - \mathbf{r}_0)^2 + \dots, \quad (2)$$

where  $\mathbf{r}$  and  $\mathbf{r}_0$  are the instantaneous and equilibrium positions of oxygen, respectively, in our case. Usually spin-phonon coupling is a second-order effect since the linear contribution is canceled out by the symmetric oscillation of ions around equilibrium positions. However, some local asymmetric structures would cause the linear part to be finite, such as the buckled  $\text{CuO}_2$  plane in  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ .<sup>27</sup> Similarly, in  $\text{Na}_x\text{CoO}_2$ , the oxygen and cobalt ions are not in

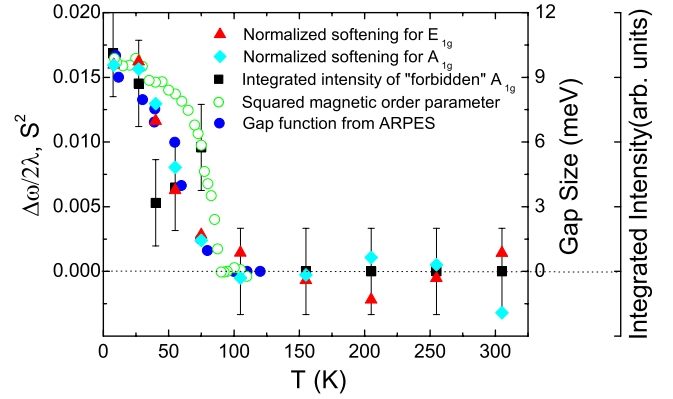


FIG. 4. (Color online) Temperature dependence of phonon softening  $\Delta\omega$  for the  $E_{1g}$  (red triangles) and  $A_{1g}$  (cyan diamonds) modes, and the integrated intensity of the forbidden  $A_{1g}$  mode in the  $xy$  channel (black squares). For details on  $\lambda$ , see text. The open green circles represent the squared magnetic order parameter  $S^2$  (Ref. 29), and the filled blue circles the gap function at the Fermi surface (Ref. 12).

the same plane. The oscillation of oxygen ions is expected to have a strong effect on magnetic interaction  $J$ . The phonon softening due to the spin-phonon coupling can be expressed as<sup>28,29</sup>

$$\Delta\omega = -\lambda \langle \mathbf{S}_i \cdot \mathbf{S}_{i+1} \rangle = 2\lambda S^2, \quad (3)$$

where  $\lambda$  is the spin-phonon coupling coefficient,  $\langle \mathbf{S}_i \cdot \mathbf{S}_{i+1} \rangle$  the average for adjacent spin pairs, and  $S^2 = (M/2g\mu_B)^2$  the squared magnetic order parameter. In evaluating  $\langle \mathbf{S}_i \cdot \mathbf{S}_{i+1} \rangle$  in the last step of Eq. (3), neutron diffraction result by Gaspárovic *et al.*<sup>9</sup> was used. In Fig. 4, measured  $S^2$  for  $\text{Na}_{0.5}\text{CoO}_2$  (open green circles)<sup>9</sup> is compared with the scaled phonon softening for the  $E_{1g}$  (red triangles) and  $A_{1g}$  (cyan diamonds) modes. While both  $\Delta\omega$  and  $S^2$  appear below  $T_{c1}$ , the softening is slower and less mean-field-like than the squared magnetic order parameter, namely, Eq. (3) is not perfectly followed. It is not clear whether this is due to  $\text{Na}_{0.5}\text{CoO}_2$  not being an insulator above the 46 K metal-insulator transition. If one nevertheless applies Eq. (3) to  $\text{Na}_{0.5}\text{CoO}_2$  at 8 K, which is then an insulator, the spin-phonon coupling coefficient  $\lambda$  is estimated as  $30 \text{ cm}^{-1}$  for the  $A_{1g}$  mode and  $41 \text{ cm}^{-1}$  for the  $E_{1g}$  mode, respectively. For comparison,  $\lambda$  is  $-50 \text{ cm}^{-1}$  in  $\text{CuO}$ ,<sup>29</sup>  $6$  and  $9 \text{ cm}^{-1}$  for two phonon modes in  $\text{Y}_2\text{Ru}_2\text{O}_7$ ,<sup>30</sup> and  $|\lambda|$  is less than  $3 \text{ cm}^{-1}$  for antiferromagnets in the rutile structure such as  $\text{FeF}_2$ ,  $\text{MnF}_2$ , and  $\text{NiF}_2$ .<sup>28</sup> Thus, the spin-phonon coupling in  $\text{Na}_{0.5}\text{CoO}_2$  is very strong.

The spin-phonon coupling is a *dynamical* spin-lattice interaction. At a magnetic transition, *static* spin-lattice interaction is also possible, which is usually referred to as magnetoelastic effect. The effect requires no phonon softening, but a static change of local structure. In addition to the phonon softening, we observed in this work that the  $A_{1g}$  mode in the forbidden  $xy$  channel also appears below  $T_{c1}$  in  $\text{Na}_{0.5}\text{CoO}_2$ , see Fig. 2(b). The violation of the Raman selection rules mentioned above for the triangular layers requires a structural distortion in the edge-shared  $\text{CoO}_6$  to break lattice sym-

metry of the high temperature phase. Qualitatively, the integrated intensity of the forbidden  $A_{1g}$  mode is proportional to the distortion at low temperatures. In Fig. 4, the integrated intensity of the forbidden mode is plotted as the black squares. It follows the general trend of  $\Delta\omega$ , except that there appears a dip around  $T_{c2}$ . However, more sensitive experiments are called for to establish the statistical significance of the dip. Magnon scattering was suggested as the origin of the forbidden  $A_{1g}$  mode in view that the mode appears only below the magnetic transition. However, this explanation has difficulty for the same mode in the allowed  $xx$  channel at all measured temperatures.

In Fig. 4, the single-particle gap function (filled blue circles) from the ARPES measurements<sup>12</sup> is also plotted. Different from magnetic order parameter, it traces the phonon softening  $\Delta\omega$  very well. On the other hand, the metal-insulator transition at  $T_{c2}$  has no detectable effect on either  $\Delta\omega$  or the gap function. Although the gap is opened only at the  $a_{1g}$  Fermi surface of the Co ions, the Na ordering at  $\sim 350$  K was invoked to provide a nesting condition for the Fermi surface.<sup>12</sup> However Qian *et al.* also noticed that their observed gap is less anisotropic than expected from such a nesting scenario and that the gap size is rather soft compared to many charge-density wave systems. In addition, the Fermi surface geometry does not share the twofold symmetry of the Na supercell.<sup>12</sup> Thus, our observed structural transition directly involving  $\text{CoO}_6$  at the same temperature offers a promising alternative mechanism for the band folding. Similarly, the supercell needed for explanation of the NMR results at  $T_{c1}$  (Ref. 11) may come instead from the distortion of the  $\text{CoO}_6$  octahedra. We notice that electron diffraction experiments at 100 K detected from the Na layers another tripled superlattice pattern which, however, disappears at 20 K.<sup>4,10</sup> Whether the tripled superlattice pattern has anything to do with our observed  $\text{CoO}_6$  distortion, which persists

down to our lowest measurement temperature at 8 K, is not obvious.

#### IV. CONCLUSIONS

In summary, our polarized Raman measurements of  $\text{Na}_{0.5}\text{CoO}_2$  single crystal have shed light on the multiple phase transitions in the interesting material. Above  $T_{c1} \approx 83$  K, only conventional anharmonic effect was observed. The softening of the  $A_{1g}$  and  $E_{1g}$  optical phonon modes was observed below  $T_{c1}$ , accompanied by the  $A_{1g}$  mode in the forbidden  $xy$  Raman channel. Our results indicate a structural transition at  $T_{c1}$  which breaks the local lattice symmetry of the  $\text{CoO}_6$  octahedra. The spin-phonon coupling in  $\text{Na}_{0.5}\text{CoO}_2$  is among the strongest of magnetic materials. The closely related order parameters of the structural distortion and phonon softening in the  $\text{CoO}_6$  layers as well as the magnetic and electronic transitions involving electrons of Co ions suggest a common origin for these transitions. The structural condition for the nesting Fermi surface scenario which was invoked as the mechanism for the magnetic transition and the partial gapping of the Fermi surface at  $T_{c1}$  is more likely the structural distortion discovered in this work in the Co layers than the orthorhombic Na ordering at  $\sim 350$  K. If  $\text{Na}_{0.5}\text{CoO}_2$  is indeed more appropriate as the parent compound of the superconducting  $\text{Na}_{0.35}\text{CoO}_2 \cdot 1.3\text{H}_2\text{O}$ ,<sup>5,6</sup> it may be difficult to exclude a lattice contribution to focus on a purely electronic superconducting mechanism.

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